...previously, in 8.972...

Patterns in the Solar system



Patterns in the Solar system



Exoplanet discoveries





Direct imaging

b



A

Neuhauser et al.

Direct imaging



Chauvin et al.

The contrast problem







Only works for hot, distant planets...





...and no direct measurement of M, R

Spectroscopy (Doppler shift)

Astrometry (angular shift)



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• Spectroscopy (Doppler shift)

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$$\Delta V_{\rm max} = \left(\frac{2\pi G}{P}\right)^{1/3} \frac{M_P \sin I}{(M_P + M_S)^{2/3}} \\\approx (12 \text{ m s}^{-1}) \left(\frac{P}{12 \text{ yr}}\right)^{-1/3} \left(\frac{M_P \sin I}{M_{\rm Jup}}\right) \left(\frac{M_S}{M_{\rm Sun}}\right)^{-2/3}$$

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state of the art: 0.5 m/s (iodine cell, dual-fiber)

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sin(I) ambiguity; radius unknown

Astrometry (angular shift)

$$\Delta \theta_{\text{max}} = \left(\frac{M_P/M_S}{d}\right) \left(\frac{G(M_P + M_S)P^2}{4\pi^2}\right)^{1/3}$$
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gets harder with distance; radius unknown

$$\frac{\Delta F_{\text{max}}}{F} \approx \left(\frac{R_P}{R_S}\right)^2 \approx 10^{-2} \left(\frac{R_P/R_S}{R_{\text{Jup}}/R_{\text{Sun}}}\right)^2$$
duration $\approx \frac{R_S}{(2\pi a/P)} \approx 14 \text{ hr } \left(\frac{R_S}{R_{\text{Sun}}}\right) \left(\frac{P}{11 \text{ yr}}\right)^{1/3}$
Prob. $\approx 0.1\% \left(\frac{R_S/R_{\text{Sun}}}{a/5 \text{ AU}}\right)$

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duration $\approx \frac{R_S}{(2\pi a/P)} \approx 1.3 \text{ hr } \left(\frac{R_S}{R_{\text{Sun}}}\right) \left(\frac{P}{3 \text{ days}}\right)^{1/3}$
Prob. $\approx 10\% \left(\frac{R_S/R_{\text{Sun}}}{a/0.05 \text{ AU}}\right)$

Photometry (transits)

OGLE-TR-56 P=1.21190 (days)







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learn mass, incl, radius, temperature, more!





Gravitational lensing

OGLE 2005-BLG-390

