

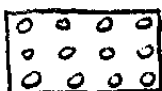
THERMAL PROPERTIES OF MATTER

I. PHASES OF MATTER

(A) SOLIDS, LIQUIDS AND GASES

SOLIDS

• CRYSTAL STRUCTURE



- Rigid, Regular order of atoms
- Tightly-bound - don't "flow"
- Small volume change with P & T
 - e.g., Block of Fe
- amorphous structure
 - Irregular order
 - don't "flow"

LIQUIDS

- "Flow" - not rigid
- Larger change in V with P & T .

GASES

- Take "shape" of container
- Atoms/Molecules move-around freely (randomly)
- large V change with P & T .

(B) "Common Bond"

- Relationship between each can be qualitatively understood with one principle: (Kinetic Energy) vs. (Interaction Energy)

SOLIDS

$$K.E. \ll I.E.$$

LIQUIDS

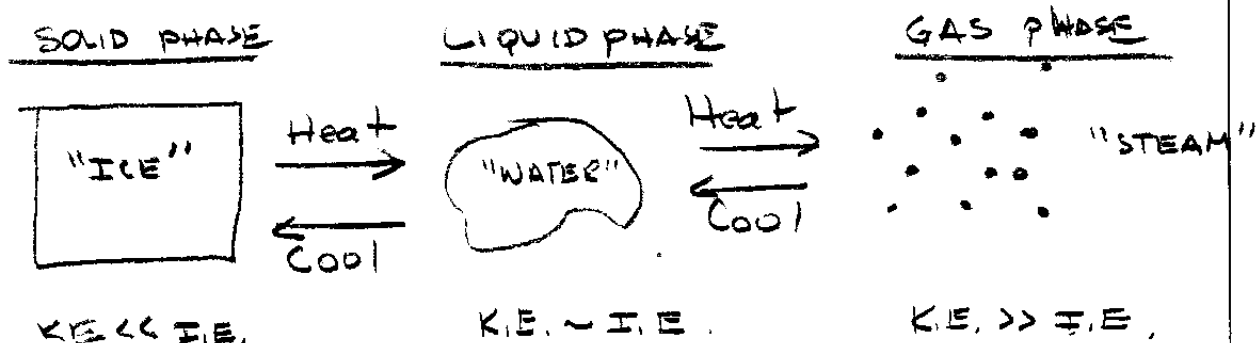
$$K.E. \sim I.E.$$

GASES

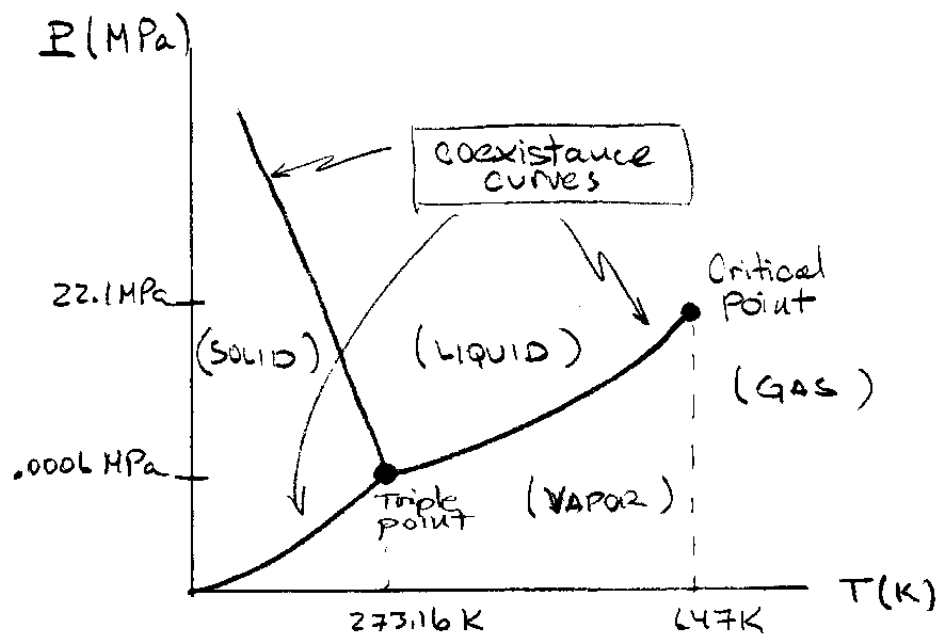
$$K.E. \gg I.E.$$

THERMAL PROPERTIES OF MATTER

(C) PHASE TRANSITIONS

Example: H_2O 

(D) Phase Diagrams

Example: H_2O 

- Condensation
- Sublimation

THERMAL PROPERTIES OF MATTER

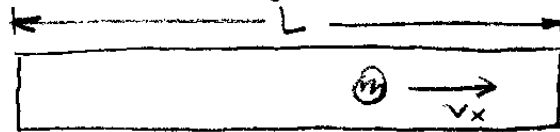
II. KINETIC THEORY (Boltzmann/Maxwell, 19th cy.)

(A) Democritus "Atomists" (ca 300 B.C.)

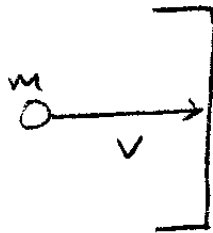
Thompson/Rutherford (ca. 1900)

Boltzmann/Maxwell (ca. 1850s)

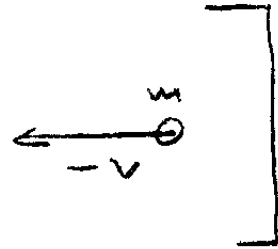
(B) "1-dimensional gas"



$$\Delta t = 2L/v_x$$



$$p_1 = mv_1$$

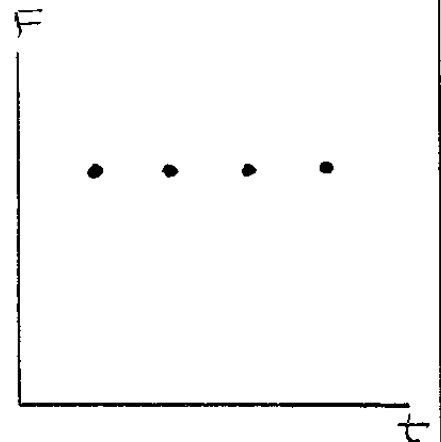


$$p_2 = mv_2$$

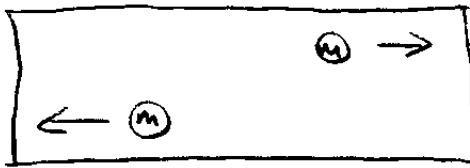
$$\begin{aligned}\Delta p &= p_2 - p_1 \\ &= m(v_2 - v_1)\end{aligned}$$

$$\Delta p = 2mV$$

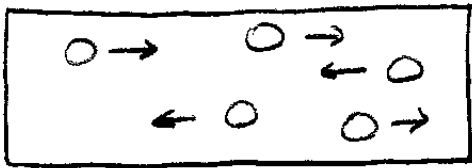
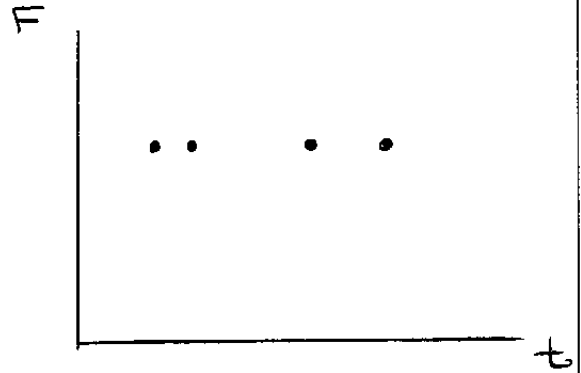
$$F = \frac{\Delta p}{\Delta t} = \frac{2mV}{(2L/V)} = \frac{mV_x^2}{L}$$



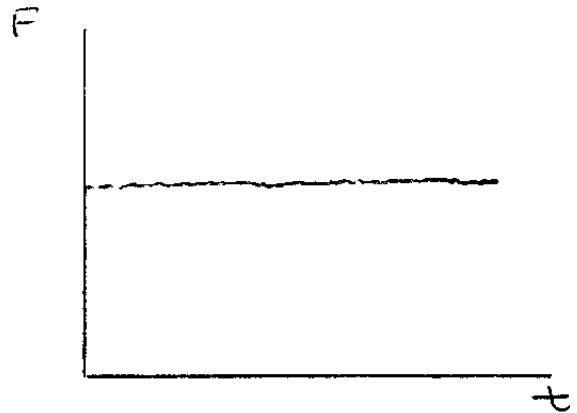
THERMAL PROPERTIES OF MATTER



$$\langle F \rangle = \frac{Nm \langle v_x^2 \rangle}{L}$$

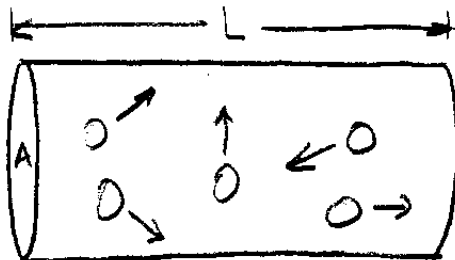


$$\langle F \rangle = \frac{Nm \langle v_x^2 \rangle}{L}$$



$\langle P_M \rangle$ ← "microscopic pressure"

$$\langle P_M \rangle = \frac{\langle F \rangle}{A} = \frac{Nm \langle v_x^2 \rangle}{LA}$$



$$\langle P_M \rangle = \frac{Nm \langle v^2 \rangle}{3LA}$$

but $\langle v^2 \rangle = \langle v_x^2 + v_y^2 + v_z^2 \rangle \Rightarrow \langle v_x^2 \rangle = \frac{1}{3} \langle v^2 \rangle$

$$\langle P_M \rangle = \frac{Nm \langle v^2 \rangle}{3LA} = \frac{Nm \langle v^2 \rangle}{3V}$$

THERMAL PROPERTIES OF MATTER

$$\langle P_M \rangle V = \frac{1}{3} N m \langle v^2 \rangle$$

Recall that

$$K.E. = \frac{1}{2} m v^2$$

So

$$\langle K.E. \rangle = \frac{1}{2} m \langle v^2 \rangle$$

$$\Rightarrow m \langle v^2 \rangle = 2 \langle K.E. \rangle$$

$$\langle P_M \rangle V = \frac{2}{3} \langle K.E. \rangle$$

From Ideal Gas Law -

$$PV = N k_B T$$

Postulate that

$$P = \langle P_M \rangle$$

$$\Rightarrow PV = \langle P_M \rangle V$$

$$N k_B T = \frac{2}{3} N \langle K.E. \rangle$$

$$T = \frac{2}{3} \frac{\langle K.E. \rangle}{k_B} \quad \text{A Microscopic Definition of Temperature!}$$

$$\langle K.E. \rangle = \frac{3}{2} k_B T = \frac{1}{2} m \langle v^2 \rangle$$

$$\Rightarrow \langle v^2 \rangle = \frac{3 k_B T}{m}$$

$$V_{rms} \equiv \sqrt{\langle v^2 \rangle} = \sqrt{\frac{3 k_B T}{m}}$$