

13.1 $100\text{ g } \text{H}_2\text{O}$

$20^\circ\text{C} \rightarrow 40^\circ\text{C} \Rightarrow \Delta T = 20\text{K}$

How much heat transmitted?

1 cal = Q to raise 1 g H_2O by 1°C

$\Rightarrow$ here $Q = (1\text{ cal/g} \cdot 1^\circ\text{C}) (100\text{ g}) (20^\circ\text{C})$

$Q = 2000\text{ cal} = 2\text{ kcal}$

13.3 $10\text{ g } \text{H}_2\text{O} @ 20^\circ\text{C}$

How much Q_{out} to lower to 0°C ?

$\Delta T = 20^\circ\text{C}$

$Q = \frac{1\text{ cal}}{1\text{ g } ^\circ\text{C}} \times 10\text{ g} \times -20^\circ\text{C} =$

$200\text{ cal removed} = Q$

13.5 $30\text{ L } \text{H}_2\text{O}$

How much ΔT for 500 kcal ?

$30\text{ L} = V$ need mass.

$\text{H}_2\text{O}: 1\text{ g} = 1\text{ mL}$ (density)

$\frac{30\text{ L}}{1\text{ L}} \left| \frac{1000\text{ mL}}{1\text{ L}} \right| \left| \frac{1\text{ g}}{1\text{ mL}} \right| = 30,000\text{ g} = m$

$500 \times 10^3\text{ cal} = \left(\frac{1\text{ cal}}{1\text{ g } ^\circ\text{C}} \right) (30,000\text{ g}) \Delta T$

$\Delta T = 16.7^\circ\text{C}$

13.9

100g H_2O @ $100^\circ C$ $\leftarrow$ ①

added to

100g @ $20^\circ C$ $\leftarrow$ ②

What is T_{final} ?

Conservation of Energy

$$\Delta Q_1 + \Delta Q_2 = 0$$

$$\Delta Q_1 = m_1 c (T_f - T_1)$$

$$\Delta Q_2 = m_2 c (T_f - T_2)$$

$$m_1 c (T_f - T_1) + m_2 c (T_f - T_2) = 0$$

$$m_1 (T_f - T_1) + m_2 (T_f - T_2) = 0$$

$$m_1 T_f - m_1 T_1 + m_2 T_f - m_2 T_2 = 0$$

$$T_f (m_1 + m_2) = m_1 T_1 + m_2 T_2$$

$$T_f = \frac{m_1 T_1 + m_2 T_2}{m_1 + m_2} = \frac{(100g)(100^\circ C) + (100g)(20^\circ C)}{200g}$$

$$T_f = 60^\circ C$$

13.31

Al

$$c_A = 910 \text{ J/kg} \cdot \text{K}$$

$$T_A = 473 \text{ K}$$

$$m_A = ?$$

H₂O

$$c = 4186 \text{ J/kg} \cdot \text{K} \quad (\text{Table 13.3})$$

$$T_w = 20^\circ\text{C} = 293 \text{ K}$$

$$m_w = 4.95 \text{ kg}$$

$$T_f = 300 \text{ K}$$

Conservation
of Energy

$$\Delta Q_A + \Delta Q_w = 0$$

$$m_A c_A (T_f - T_A) = -m_w c_w (T_f - T_w)$$

$$m_A = \frac{m_w c_w (T_f - T_w)}{c_A (T_f - T_A)} = \frac{(4.95 \text{ kg})(4186 \text{ J/kg} \cdot \text{K})(300 \text{ K} - 293 \text{ K})}{(910 \text{ J/kg} \cdot \text{K})(300 \text{ K} - 473 \text{ K})}$$

$$m_A = 0.92 \text{ kg}$$

13.35

Cu

Olive Oil

Glass

$$m = 200.5 \text{ g}$$

$$m = 118.1 \text{ g}$$

$$m = 84.0 \text{ g}$$

Table 13.3

$$c_c = 0.093 \text{ kcal/kg} \cdot \text{K}$$

$$c = 0.471 \text{ kcal/kg} \cdot \text{K}$$

$$c_g = 0.2 \text{ kcal/kg} \cdot \text{K}$$

$$T_c = 20^\circ \text{C}$$

$$T_o = 20^\circ \text{C}$$

$$T_g = 300^\circ \text{C}$$

$$\leftarrow T_f = ? \rightarrow$$

$$\Delta Q_c + \Delta Q_o + \Delta Q_g = 0$$

$$\Delta Q_c = m_c c_c \Delta T_c$$

$$\Delta Q_o = m_o c_o \Delta T_o$$

$$\Delta Q_g = m_g c_g \Delta T_g$$

$$m_c c_c (T_f - T_c) + m_o c_o (T_f - T_o) + m_g c_g (T_f - T_g) = 0$$

$$T_f = \frac{m_c c_c T_c + m_o c_o T_o + m_g c_g T_g}{m_c c_c + m_o c_o + m_g c_g}$$

$$T_f = 72^\circ \text{C}$$

$$= \frac{(200.5)(0.093)(20) + (118.1)(0.471)(20) + (84)(0.2)(300)}{(200.5)(0.093) + (118.1)(0.471) + (84)(0.2)}$$

$$T_f = 71.7^\circ \text{C}$$

~~13.55, 13.57, 13.59, 13.65, 13.87~~~~14.1, 14.3, 14.29, 14.43, 14.57~~~~15.5, 15.9, 15.11~~

4.11

13.551000 cm³ block of ice @ 0°C

Q to melt?

$$Q = mL_f$$

$$m = ?$$

$$V = 1000 \text{ cm}^3$$

$$m = \rho V$$

$$\rho_{\text{ice}} = 920 \text{ kg/m}^3 \quad (\text{pg. 358})$$

$$L_f = 333.7 \text{ kJ/kg} \quad (\text{pg. 546})$$

$$m = \left(920 \frac{\text{kg}}{\text{m}^3} \right) \left(1000 \text{ cm}^3 \times \left(\frac{1 \text{ m}}{100 \text{ cm}} \right)^3 \right)$$

$$m = 0.92 \text{ kg}$$

$$Q = (0.92 \text{ kg})(333.7 \text{ kJ/kg}) = 307 \text{ kJ}$$

$$Q = 3.07 \times 10^5 \text{ J}$$

13.57

Q needed to melt Cu @ 1356 K?

First heat to melting temp, then melt.

$$Q = mc\Delta T$$

$$Q = mL_f$$

$$T_{\text{melt}} = 1083^\circ\text{C} = 1356 \text{ K} \quad (\text{Table 13.6}) \Rightarrow \Delta T = 0$$

$$Q = mL_f \quad m = 0.2 \text{ kg} \quad L_f = 205 \text{ kJ/kg}$$

$$= (0.2 \text{ kg})(205 \text{ kJ/kg}) = 41 \text{ kJ} = Q$$

13.59 Initially

ICE

$$m_I = ?$$

$$T = 0^\circ\text{C}$$

$$L_f = 333.7 \text{ kJ/kg}$$

Finally

WATER @ 0°C

WATER

$$m_W = 0.50 \text{ kg}$$

$$T_W = 20^\circ\text{C}$$

$$c_W = 4.186 \text{ kJ/kg}\cdot\text{K}$$

Ice gains heat: $Q = mL_f$

H_2O loses heat: $Q = mc\Delta T$

$$\Delta T = 0 - 20 = -20 \text{ K}$$

$$\Delta Q_{\text{ICE}} + \Delta Q_{\text{H}_2\text{O}} = 0$$

$$m_I L_f + m_W c_W \Delta T_W = 0$$

$$m_I = \frac{-m_W c_W \Delta T_W}{L_f} = \frac{-(0.50 \text{ kg})(4.186 \text{ kJ/kg}\cdot\text{K})(-20 \text{ K})}{333.7 \text{ kJ/kg}}$$

$$m_I = 0.125 \text{ kg}$$

13.65

$$\text{Hg: } m = 0.50 \text{ kg}$$

$$c = 138 \text{ J/kg}\cdot\text{K}$$

$$T_i = 240 \text{ K}$$

$$T_{\text{boil}} = 357^\circ\text{C} = 630 \text{ K} \quad (\text{Table 13.6})$$

$$L_v = 296 \text{ kJ/kg} = 296 \times 10^3 \text{ J/kg}$$

Heat to vaporize?

$$Q_{\text{tot}} = \underset{\substack{\uparrow \\ \text{raise temp}}}{mc\Delta T} + \underset{\substack{\uparrow \\ \text{vaporize}}}{mL_v}$$

$$Q_{\text{tot}} = (0.50 \text{ kg})(138 \text{ J/kg}\cdot\text{K})(630 - 240 \text{ K}) + (0.50 \text{ kg})(296 \times 10^3 \text{ J/kg})$$

$$= 174910 \text{ J}$$

$$Q = 175 \text{ kJ}$$

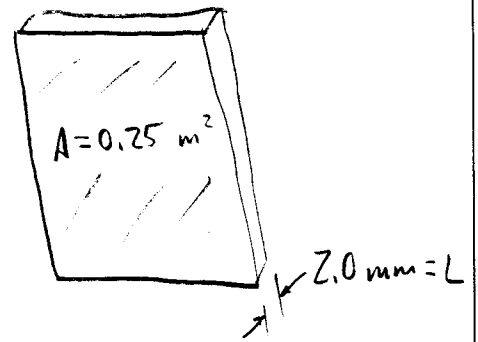
13.87

$$k_T = 0.80 \text{ W/m}\cdot\text{K}$$

$$T_{\text{out}} = -18^\circ\text{C}$$

$$T_{\text{in}} = 21^\circ\text{C}$$

What is Q/sec ?



H = heat transferred per time:

$$= -k_T A \frac{\Delta T}{L} = \frac{-(0.80 \text{ W/m}\cdot\text{K})(0.25 \text{ m}^2)(-18 - 21 \text{ K})}{0.002 \text{ m}}$$

$$H = 3900 \text{ W} = 3.9 \text{ kW}$$

So 3.9 kJ per second heat is transferred