

Thermodynamics

Relates internal (heat) energy and its flow to temperature and work

Heat flows from "hot" $\rightarrow$ "cold"

Temperature = measure of "hotness" [Kelvin]

- $T = 0 \text{ K}$ ("absolute zero") when no more heat can be extracted from system

$$= 273.16 \text{ K at } 0^\circ\text{C} \text{ (} 32^\circ\text{F)}$$

"Zeroth" Law of TD:

"If two bodies are in thermal eqm. with a third, they are in thermal eqm. with each other."

i.e. if $T_c = T_A$ and $T_c = T_B$, then $T_A = T_B$



no heat flow

$$T_A = T_B$$

Temperature: Measurement, Defining a Scale

Zeroth law $\rightarrow$ unique temp. for any system in eq. m.

Definition $\rightarrow$ If $T_A > T_B$, heat flows $A \rightarrow B$

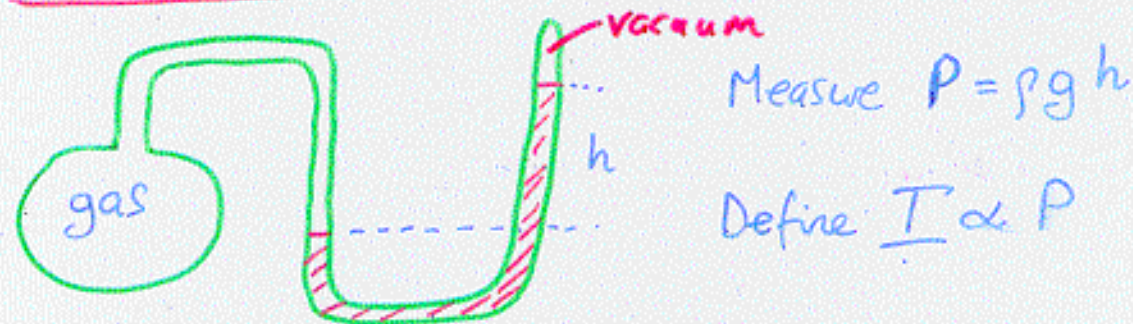
Can use physical properties to define a scale, but which?

- density, pressure, electrical resistance ?
 thermal expansion gas can go $\uparrow$ or $\downarrow$ as $T \uparrow$

We choose:

① H_2O triple-point has $T_3 = 273.16 \text{ K}$
 $(\Rightarrow T_{\text{boil}} - T_3 = 100 \text{ K} = 100^\circ\text{C})$

② Constant-volume Gas Thermometer:

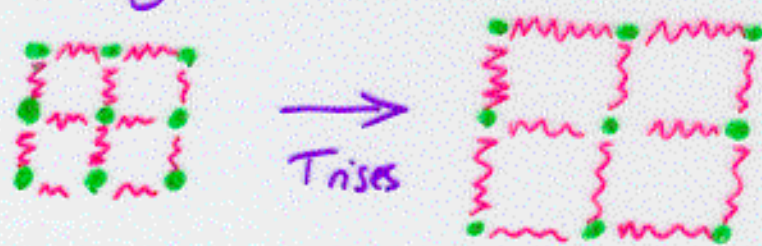


$$\text{So } \frac{T}{T_3} = \frac{P}{P_3} \Rightarrow T = (273.16) \frac{P}{P_3}$$

Good news: Any gas gives same value for T as $n \rightarrow 0$

Thermal Expansion of Solids + Liquids

- Most solids + liquids increase size as $T \uparrow$
(i.e. their density $\downarrow$)



inter-atomic distances increase as heat is absorbed

e.g. railroad tracks, dental fillings, bimetallic strip

Coefficient of linear expansion α : $\frac{\Delta L}{L} = \alpha \Delta T$

- fractional length change per Kelvin temp. change $[1/K]$

Note: every dimension changes, e.g. hole in solid also increases in size.

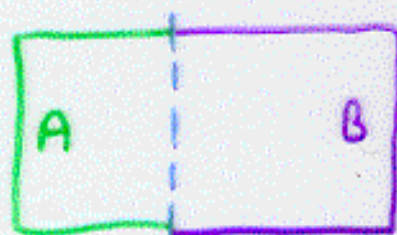
For a cube of side x , change in volume $V = x^3$

$$\text{is } \frac{dV}{dT} = \frac{dV}{dx} \cdot \frac{dx}{dT} = 3x^2 \cdot \alpha x = 3\alpha V$$

$\Rightarrow$ Coeff. of volume expansion $\frac{dV}{V} \equiv \beta = 3\alpha$

- fractional vol. change per Kelvin. $[1/K]$

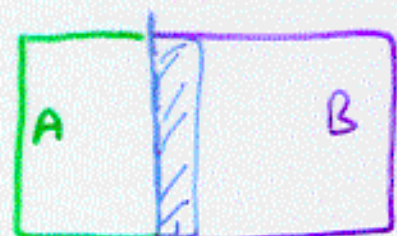
Temperature and Heat Transfer



thermal interaction
heat exchange if $T_A \neq T_B$

diathermic wall (conducts heat)

cf.



A, B push piston around
 $\Rightarrow$ work exchanged (force moves point of app.)

piston (insulated)

Heat Capacity:

If body absorbs heat energy Q (Joule) with no change in state,

$$Q = m C \Delta T : C \equiv \text{specific heat capacity [J/kg/K]}$$

e.g. water: $C = 4190 \text{ J/kg/K} = 1 \text{ Calorie}$

Example: Aluminum can, $m = \overset{100g}{\cancel{200g}}$, $T = 0^\circ\text{C}$
filled with 2.00g water at 80°C .

- what is final temp. of mixture? ($C_{Al} = 900 \text{ J/kg/K}$)

Use: Heat gained by can = Heat lost by water

$$T_f(\text{can}) = T_f(\text{water})$$

Heat of Transformation (L)

= heat absorbed / released for a change of state with no change in temp:

e.g. ice at $0^{\circ}\text{C} \rightarrow$ water at $0^{\circ}\text{C} : L = 333 \text{ kJ/kg}$

water at $100^{\circ}\text{C} \rightarrow$ steam at $100^{\circ}\text{C} : L = 2256 \text{ kJ/kg}$

Note: during transformation, mixture is at eqm. since $T_1 = T_2$

Example: Insulated container, 2kg ice at -5°C ,
heater inputs heat at 5 kW

① To bring ice to 0°C , $Q = 2 \text{ kg} \times C_{\text{ice}} \times (5^{\circ}\text{C})$

$$= 2 \times 2220 \times 5 = 22.2 \text{ kJ. Time taken} = \frac{22.2}{5} = \underline{4.44 \text{ s}}$$

② To melt ice, $Q = 2 \text{ kg} \times L_{\text{ice}} = 2 \times 333 \times 10^3 = 666 \text{ kJ}$

$$\text{Time taken} = \frac{666}{5} = \underline{133.2 \text{ s}}$$

③ After 180s, time to heat water from 0°C to $T_f = (180 - 133.2 - 4.44)$
 $= 42.36 \text{ s} \Rightarrow \text{heat input} = 5 \text{ kW} \times 42.36 = 211.8 \text{ kJ}$

$$\therefore \text{Final temp } T_f = 0 = \frac{\Delta Q}{C_{\text{water}}} = \frac{211.8 \text{ kJ}}{4190} = \underline{50.55^{\circ}\text{C}}$$