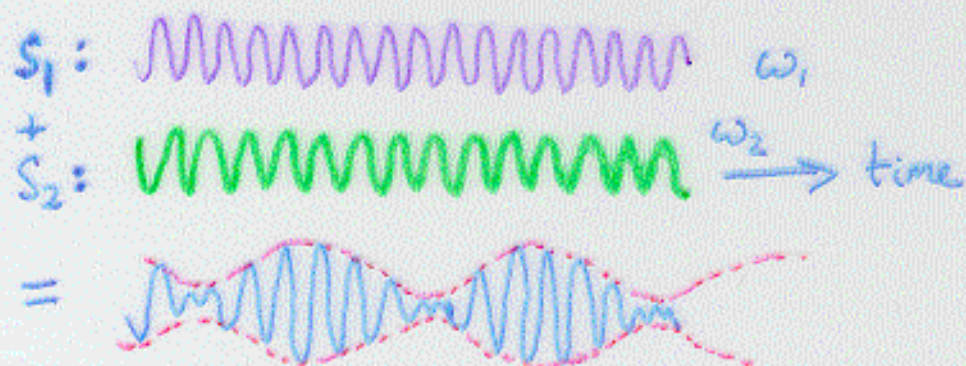


Beat Frequency: Add 2 waves close in frequency



2nd wave gradually falls in and out of phase with first

$\Rightarrow$ periodic "beats" of constructive/destructive interference

$$\begin{aligned} \text{Resulting } S_1 + S_2 &= S_m \cos \omega_1 t + S_m \cos \omega_2 t \\ &= 2S_m \cos \underbrace{\frac{1}{2}(\omega_1 - \omega_2)t}_{\omega_{\text{beat}}} \cos \underbrace{\frac{1}{2}(\omega_1 + \omega_2)t}_{\omega_{\text{av}}} \end{aligned}$$

Resulting oscillation is at average ang. frequency but with amplitude modulated at ω_{beat} .

Sound intensity $\propto (\text{amplitude})^2$ is max. when $\cos(\omega_{\text{beat}} t) = \pm 1$

$$\Rightarrow \text{\# of beats / s } \underline{f_{\text{beat}} = f_1 - f_2}$$

- can be used to tune instruments
- can hear beats from twin-engine aircraft when engines' rpm is close, but not identical.