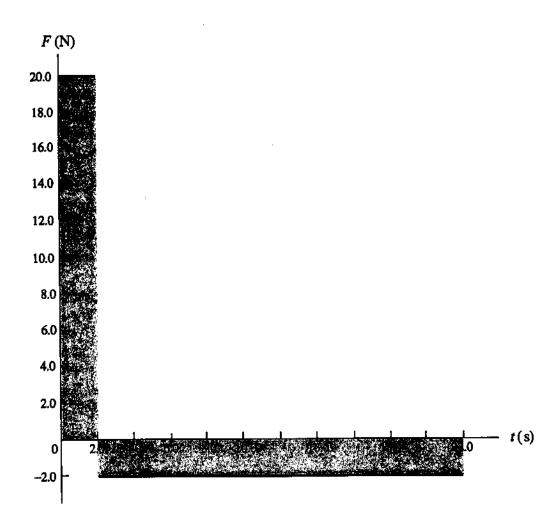
Taking the initial direction of motion of the wad of clay (of mass m) as positive, then before its impact with the wall  $v_i = +10 \, \mathrm{m/s}$ , and afterwards  $v_i = 0$ . The change in momentum for the clay is then

$$\Delta p = mv_i - mv_i = -(1.0 \text{ kg})(10 \text{ m/s}) = -10 \text{ N·s},$$

which, according to Eq. (7.4), is equal to the impulse delivered on the clay by the wall.

7.7 The first force  $F_1$  is along the positive x-direction and delivers an impulse  $F_1\Delta t_1=(+20\,\mathrm{N})\times(2.0\,\mathrm{s})=+40\,\mathrm{N}\cdot\mathrm{s}$ ; while the second force  $F_2$  is along the negative x-direction, delivering an impulse  $F_2\Delta t_2=(-2.0\,\mathrm{N})(20\,\mathrm{s})=-40\,\mathrm{N}\cdot\mathrm{s}$ . Both impulses are represented by the corresponding shaded areas in the force vs time plot shown below, with the area below the t-axis counted as negative. The net impulse experienced by the body is then  $F_1\Delta t_1+F_2\Delta t_2=+40\,\mathrm{Ns}-40\,\mathrm{Ns}=0$ ; so there is no net change in the momentum of the body, whose final momentum  $p_t$  must then be the same as its initial value:

$$p_{\rm f} = p_{\rm i} = mv_{\rm i} = (1.0\,{\rm kg})(10\,{\rm m/s}) = 10\,{\rm kg\cdot m/s}$$
.



Compared with a karate chop, a boxer's punch is softer (i.e. with a smaller value of  $F_{av}$ ) but lasts a longer time interval. Thus the first graph, with  $F_{av} \approx 400\,\mathrm{N}$  and  $\Delta t \approx 0.12\,\mathrm{s} - 0.02\,\mathrm{s} = 0.1\,\mathrm{s}$ , is likely a boxer's punch; while the second one, with  $F_{av} \approx 2000\,\mathrm{N}$  and  $\Delta t \approx 0.06\,\mathrm{s} - 0.04\,\mathrm{s} = 0.02\,\mathrm{s}$ , is likely a karate's chop.

The impulse represented by the first curve is approximately  $(400 \,\mathrm{N})(0.10 \,\mathrm{s}) = 40 \,\mathrm{N} \cdot \mathrm{s}$ ; while that by the second one is  $(2000 \,\mathrm{N})(0.02 \,\mathrm{s}) = 40 \,\mathrm{N} \cdot \mathrm{s}$ , roughly the same as the first one.

The karate's chop involves a peak force of about 2000 N, which is 5 times as much as that of the boxer's punch. So the karate's chop is more likely to break bones.

### <u>7.14</u>

Taking east as positive, the force of the wind is expressed as  $F(t) = +(0.025 \,\mathrm{N/s}) \,t$ . The impulse it delivered on the balloon between 0 and 0.40 s is then

$$\int_0^{0.40\,\mathrm{s}} F(t)\,dt = \int_0^{0.40\,\mathrm{s}} (0.025\,\mathrm{N/s})t\,dt = (0.025\,\mathrm{N/s}) \left[\frac{1}{2}t^2\right]_0^{0.40\,\mathrm{s}} = +2.0\times10^{-3}\,\mathrm{N\cdot s}\,.$$

The resulting change in momentum of the balloon, with mass  $m = 20.0 \,\mathrm{g} = 0.020 \,\mathrm{kg}$  and initial speed  $v_i = 0.10 \,\mathrm{m/s}$ , is  $\Delta p = mv - mv_i$ , with v its speed at  $t = 0.40 \,\mathrm{s}$ . Equate the impulse with  $\Delta p$ :  $mv - mv_i = 2.0 \times 10^{-3} \,\mathrm{N} \cdot \mathrm{s}$ , and solve for v:

$$v=v_{_{\rm i}}+rac{2.0 imes10^{-3}\,{
m N\cdot s}}{m}=0.10\,{
m m/s}+rac{2.0 imes10^{-3}\,{
m N\cdot s}}{0.020\,{
m kg}}=+0.20\,{
m m/s}$$
 ,

due east.

#### 7.21

Taking the initial direction of motion of the hammer as positive, then before the impact its initial velocity is  $v_i = +5 \,\mathrm{m/s}$ , and afterwards  $v_t = -1 \,\mathrm{m/s}$ . The change in momentum for the hammer of mass m is then  $\Delta p = m v_t - m v_i = m (v_t - v_i)$ . If this is accomplished in  $\Delta t = 1 \,\mathrm{ms} = 1 \times 10^{-3} \,\mathrm{s}$ , then from Eq. (7.2) the average force exerted by the nail on the hammer is

$$F_{\rm av} = \frac{\Delta p}{\Delta t} = \frac{m(v_{\rm f} - v_{\rm i})}{\Delta t} = \frac{(1\,{\rm kg})\left[(-1\,{\rm m/s}) - (+5\,{\rm m/s})\right]}{1\times 10^{-3}\,{\rm s}} = -6\times 10^3\,{\rm N} = -6\,{\rm kN}\,,$$

where the negative sign indicates that  $\vec{F}_{av}$  is against the initial direction of motion of the hammer. According to Newton's Third Law, the force exerted by the nail on the hammer is  $-F_{av} = +6 \,\mathrm{kN}$ , in the initial direction of motion of the hammer.

CHAPTER 7 MOMENTUM AND COLLISIONS

# 264

## 7.39

The initial momentum of the system consisting the person (P) and the boat (B) is  $\vec{\mathbf{p}}_i = 0$ , since neither was moving. As the person picks up a velocity  $\vec{\mathbf{v}}_p$  with respect to the stationary water, due north (which is taken to be positive), her momentum is  $m_p \vec{\mathbf{v}}_p$ . Meanwhile, the boat is moving at a velocity  $\vec{\mathbf{v}}_p$ , resulting in a momentum of  $m_p \vec{\mathbf{v}}_p$ . The total momentum of the system is now  $\vec{\mathbf{p}}_t = m_p \vec{\mathbf{v}}_p + m_p \vec{\mathbf{v}}_p$ . Conservation of momentum requires that  $\vec{\mathbf{p}}_i = \vec{\mathbf{p}}_t$ , which becomes  $0 = m_p v_p + m_p v_p$  in scalar form. Solve for  $v_p$ , the velocity of the boat:

$$v_{\rm B} = -\frac{m_{\rm P}v_{\rm P}}{m_{\rm B}} = -\frac{(50\,{\rm kg})(10\,{\rm m/s})}{150\,{\rm kg}} = -3.3\,{\rm m/s}\,,$$

where the minus sign indicates that  $\vec{\mathbf{v}}_{\rm B}$  due south, opposite in direction to  $\vec{\mathbf{v}}_{\rm P}$ .

Use conservation of momentum. The initial momentum of the system consisting of the astronaut (A), the TV camera (C), and the backpack (B) is  $\vec{\mathbf{p}}_i = 0$ . As the astronaut throws the TV camera out at a velocity  $\vec{\mathbf{v}}_{\rm C}$ , the momentum of the camera is  $m_{\rm C}\vec{\mathbf{v}}_{\rm C}$ . Meanwhile, the rest of the system (with mass  $m_{\rm A} + m_{\rm B}$ ) recoils backward at a velocity  $\vec{\mathbf{v}}$ , resulting in a momentum of  $(m_{\rm A} + m_{\rm B})\vec{\mathbf{v}}$ . The total momentum of the system is now  $\vec{\mathbf{p}}_i = m_{\rm C}\vec{\mathbf{v}}_{\rm C} + (m_{\rm A} + m_{\rm B})\vec{\mathbf{v}}$ . Conservation of momentum requires that  $\vec{\mathbf{p}}_1 = \vec{\mathbf{p}}_i$ , which in scalar form is  $p_i = 0 = p_i = m_{\rm C}v_{\rm C} + (m_{\rm A} + m_{\rm B})v$ . Take the direction of  $\vec{\mathbf{v}}_{\rm C}$  as positive and solve for v, the recoiling velocity of the astronaut (plus the backpack):

$$v = -\frac{m_{\rm C}v_{\rm C}}{m_{\rm A} + m_{\rm B}} = -\frac{(1.0\,{\rm kg})(15\,{\rm m/s})}{90\,{\rm kg} + 10\,{\rm kg}} = -0.15\,{\rm m/s},$$

where the minus sign indicates that the recoiling velocity  $\vec{\mathbf{v}}$  of the astronaut is opposite in direction to  $\vec{\mathbf{v}}_{\rm C}$ . So after the first throw the astronaut gains a speed of 0.15 m/s towards the spaceship.

Similarly, suppose that the astronaut further gains a speed of  $v_{\rm A}'$  towards the spaceship after throwing the backpack out with a speed of  $v_{\rm B}$ , then  $0=m_{\rm B}v_{\rm B}+m_{\rm A}v_{\rm A}'$ , which gives

$$v_{\rm A}' = -\frac{m_{\rm B}v_{\rm B}}{m_{\rm A}} = -\frac{(10\,{\rm kg})(10\,{\rm m/s})}{90\,{\rm kg}} = -1.1\,{\rm m/s}\,,$$

meaning that he gains another 1.1 m/s in speed toward the spaceship after tossing out the backpack.

#### 7.57

Apply conservation of momentum each time an astronaut throws or catches the asteroid (A).

For the first step, in which Neil (N) throws the asteroid at sally (S),  $p_{Ni} + p_{Ai} = 0 = p_{Nf} + p_{Af}$ , or

$$m_{\scriptscriptstyle \rm N} v_{\scriptscriptstyle \rm Nf} + m_{\scriptscriptstyle \rm A} v_{\scriptscriptstyle \rm Af} = 0 \,,$$

where  $m_{\rm N}=100\,{\rm kg},\ m_{\rm A}=0.500\,{\rm kg}$  and, taking the direction of motion of the asteroid as positive,  $v_{\rm Af}=+20.0\,{\rm m/s}$ . This gives  $v_{\rm Nf}=-0.100\,{\rm m/s}$ , opposite to the direction of motion of the asteroid.

Now the second step, in which Sally catches the asteroid. We have  $p_{At} = p'_{At} = p'_{At} + p'_{st}$ , or

$$m_{\rm A}v_{\rm Af}=(m_{\rm A}+m_{\rm S})v_{\rm Sf}',$$

where  $m_{\rm s}=50.0\,{\rm kg},\,m_{\rm A}=0.500\,{\rm kg},\,{\rm and}\,\,v_{\rm Af}=+20.0\,{\rm m/s}.$  This gives  $\,v_{\rm sf}'=+0.198\,{\rm m/s},\,{\rm in}$  the same direction of motion as that of the asteroid.

Finally, as Sally throws the asteroid back to Neil,  $p''_{Af} + p''_{Sf} = p''_{Af} + p''_{Sf} = p'_{Af} + p'_{Sf}$ , or

$$m_{\rm A} v_{\rm Af}'' + m_{\rm S} v_{\rm Sf}'' = (m_{\rm A} + m_{\rm S}) v_{\rm Sf}'$$

Plugging in the values of  $m_{\rm A}$ ,  $m_{\rm S}$ , and noting that  $v_{\rm Af}'' = -20.0 \, {\rm m/s}$  and  $v_{\rm Sf}' = +0.198 \, {\rm m/s}$ , we solve for  $v_{\rm Sf}''$ , the final velocity of Sally, to obtain  $v_{\rm Sf}'' = +0.400 \, {\rm m/s}$ .

#### 7.58

Since the two cars are of equal mass and travel at the same speed in opposite directions, their initial momenta cancel, yielding  $p_i = 0$  for the two-car system before the collision. After the collision, the final momentum of the wreckage is  $p_t = mv_t$ , where m is its total mass. Conservation of momentum then gives  $p_t = mv_t = p_i = 0$ , or  $v_t = 0$ . So the wreckage won't move after the collision.

#### 7.71

Apply conservation of momentum to the system consisting of the two billiard balls, each with mass m:

$$p_{i} = mv_{1i} + mv_{2i} = p_{i} = mv_{1f} + mv_{2f}$$
.

Also, for elastic collisions

$$v_{2i} - v_{1i} = v_{1f} - v_{2f}$$
.

Taking north as positive, then  $v_{1i} = +15.0 \,\mathrm{m/s}$  and  $v_{2i} = -10 \,\mathrm{m/s}$ . Solve for  $v_{1i}$  and  $v_{2i}$  to obtain  $v_{1i} = v_{2i} = 15 \,\mathrm{m/s}$  and  $v_{2i} = v_{1i} = -10 \,\mathrm{m/s}$ . So the two balls just exchanged their velocities as a result of their elastic collision.

CHAPTER 7 MOMENTUM AND COLLISIONS

#### 276

#### <u>7.73</u>

Since there is no external force in the horizontal direction, the momentum of the bullet-block system is conserved in the collision. The initial momentum of the system is entirely borne by the bullet:  $p_i = m_{\rm B} v_{\rm B}$ . After the collision the bullet and the clay block (C) has reached a common speed  $v_{\rm C}$ , so  $p_{\rm f} = (m_{\rm B} + m_{\rm C}) v_{\rm C}$ . Equate  $p_{\rm i}$  with  $p_{\rm f}$  to obtain

$$m_{\scriptscriptstyle \mathrm{B}} v_{\scriptscriptstyle \mathrm{B}} = (m_{\scriptscriptstyle \mathrm{B}} + m_{\scriptscriptstyle \mathrm{C}}) v_{\scriptscriptstyle \mathrm{C}} \,.$$

After the collision, the bullet-block system rises to a new height h, trading its kinetic energy  $\frac{1}{2}(m_{\rm B}+m_{\rm C})v_{\rm C}^2$  for the gravitational potential energy,  $(m_{\rm B}+m_{\rm C})gh$ :

$$\frac{1}{2}(m_{_{\mathrm{B}}}+m_{_{\mathrm{C}}})v_{_{\mathrm{C}}}^{2}=(m_{_{\mathrm{B}}}+m_{_{\mathrm{C}}})gh$$
 .

Solve the second equation for  $v_{\rm C}$ :  $v_{\rm C} = \sqrt{2gh}$ . Plug this result into the first one and solve for  $v_{\rm B}$ , the initial speed of the bullet:

$$v_{_{\rm B}} = \left(\frac{m_{_{\rm B}} + m_{_{\rm C}}}{m_{_{\rm B}}}\right) \sqrt{2gh}\,. \label{eq:vB}$$