

Final Exam Countdown

- Today: Office hours 4:30 - 6 pm
- Thurs: Problem Section
- Friday: Quiz - waves and sound
- Monday: Office hours 10-11:30 am } by appointment
2-4 pm } (email)
- Wednesday: Final Exam 8-11 am
- Probably: 6 questions, 20 points each (max. 100)

Ace the Final !

- Lecture Notes - define material (not textbook)
- Quizzes + solutions - understand your mistakes
- Lab Homeworks - " " "
- In-class examples, textbook examples
- "Quickie" review: discussion questions at ends of chapters.

Make sure you know definitions and units of  concepts.

Review: Kinematics

- Position, Velocity, Acceleration (vectors)

For constant acceleration ($\therefore$ constant net force)

$$\begin{cases} v = v_0 + at & (mv = mv_0 + Ft) \\ x = x_0 + v_0 t + \frac{1}{2}at^2 \end{cases}$$

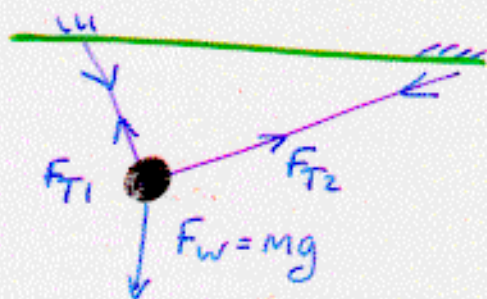
$\uparrow$
Newtonian version
 $\downarrow$

$$\Rightarrow v^2 = v_0^2 + 2ax \quad (\frac{1}{2}mv^2 = \frac{1}{2}mv_0^2 + F \cdot x)$$

Newton's Laws - make sure you know them!

- ① $\Rightarrow$ No net force $\Rightarrow$ no acceleration (object has $v=0$ or $v=\text{constant}$)

e.g. Statics : $\frac{dv}{dt} = 0$ means $\sum \vec{F} = 0$



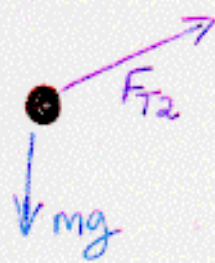
$$\text{i.e. } \sum F_x = 0$$

$$\sum F_y = 0$$

- ② Dynamics: Net force $F = \frac{d(mv)}{dt} = ma$

(e.g. if string breaks on left:

$$\text{Net } \vec{F} = m\vec{a} = \vec{F}_{T2} + m\vec{g}$$



Force, Momentum + Impulse, Kinetic Energy

Newton II $\Rightarrow \Delta(mv) = \int F \cdot dt = \underline{\text{impulse}}$

"A force acting over time changes momentum."

In collisions, Newton III $\Rightarrow F_{AB} = -F_{BA}$, also $t_A = t_B$
in contact



$$\text{So } (\Delta mv)_A = -(\Delta mv)_B$$

$\Rightarrow$ Conservation of Momentum if no external forces acting

Work and Kinetic Energy

Work $= \int F \cdot dx$: "A force acting over distance does work"

For a mass m ,

$$\text{Work} = \Delta KE = \Delta \left(\frac{1}{2} m v^2 \right)$$

Elastic collisions: Total KE conserved, Momentum Conserved

$$m_A v_{Ai} + m_B v_{Bi} = \dots \Rightarrow 2 \text{ equations for } v_A, v_B$$

$$\frac{1}{2} m_A v_A^2 + \frac{1}{2} m_B v_B^2 = \dots$$

Inelastic collisions: Momentum Conserved, but not K.E.

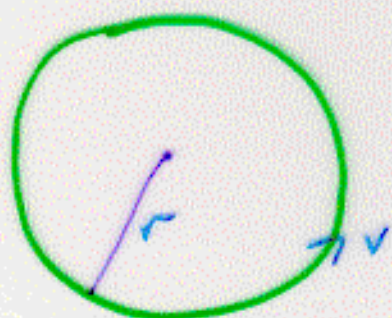
$\Rightarrow$ 1 equation for v_A, v_B and v_f

$$P_i = P_f$$

$$\bullet m_A v_A + m_B v_B = (m_A + m_B) v_f$$

Circular Motion

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Even if speed constant,
velocity changes

$$\Rightarrow \text{Centripetal Force } F_c = \frac{mv^2}{r}$$

- review problems with "effective weight" provided by F_N

e.g.



① Add up all forces
pointing towards
center.

② Set this sum = $\frac{mv^2}{r}$

e.g. At bottom of circle

$$F_N - mg = \frac{mv^2}{r}$$

$$\Rightarrow \underline{F_N} = mg + \frac{mv^2}{r} > \text{static weight } mg$$

At top:

$$F_N + mg = \frac{mv^2}{r}$$

$$\Rightarrow F_N = \frac{mv^2}{r} - mg < \text{static weight } mg$$

Note: F_N must be ≥ 0 for objects to stay in contact

Rotation and Torque

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Solid body: all parts have
same angular velocity ω [rad/s]
with $v = r\omega$

Torque $\tau = Fr \sin \theta$ about rotation center $r=0$

Center of gravity: defined such that grav. torque

$$\sum mgx = (mg)x_c \quad \text{point at which weight can be thought to act.}$$

F_w

Equations of Rotational Motion

- use Moment of Inertia $I = \sum mr^2$

Then: $\tau = I \frac{d\omega}{dt} = I\alpha \quad \left(F = m \frac{dv}{dt} \right)$

(so for $\omega = \text{constant or } 0, \Rightarrow \text{no net torque}$)

Also no external torque

$\Rightarrow$ Ang. Momentum $I\omega = \text{constant.}$ (mv)

$$\text{Rotational K.E.} = \frac{1}{2} \sum mv^2 = \sum \frac{1}{2} \underbrace{mr^2}_I \omega^2 = \frac{1}{2} I \omega^2$$