

Week 10 Reading Quiz.

1. A mechanical wave in a medium transports:
- (a) energy and momentum
 - b) energy and mass
 - c) momentum and mass
 - d) None of the above

2. The types of mechanical waves which can be found in (i) solids and (ii) liquids are:

(i) Solids

(ii) Fluids

- | | | |
|---------------|--------------|---|
| a) transverse | longitudinal | } |
| (b) both | longitudinal | |
| c) both | transverse | |
| d) both | both | |

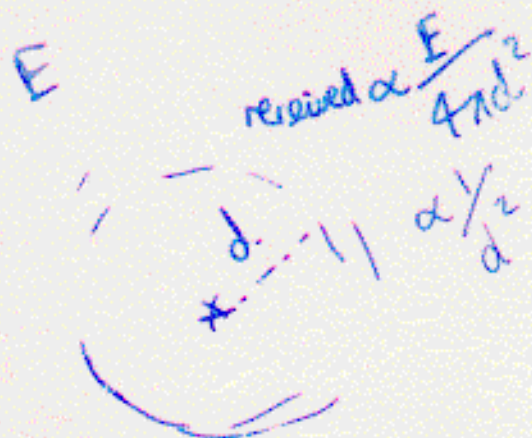
3. For a sound wave of given speed in air, when the frequency is increased, the wavelength

- a) increases
- ☒ b) decreases
- c) stays the same
- d) not enough info.

$$v = f\lambda$$

4. A firecracker explodes in mid-air and some of the sound energy is intercepted by a listener's ear at a distance of 5m. Their twin, standing 50m from the explosion, receives:

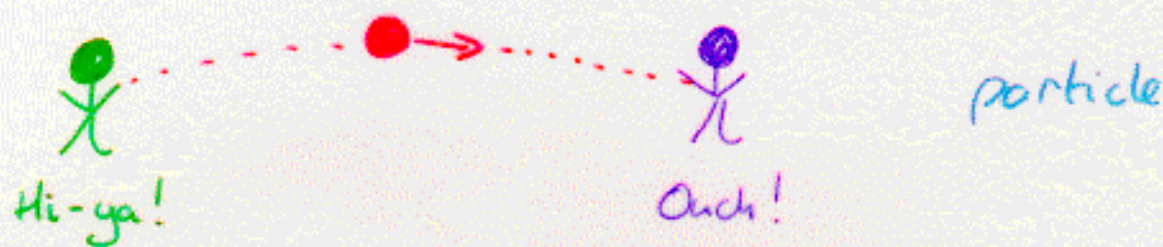
- a) $\frac{1}{10}$
- ☒ b) $\frac{1}{100}$
- c) 10^{-4}
- d) 10^{-6}



as much energy in their ears.

Mechanical Waves (Hecht ch. 11)

Waves transport energy + momentum (and information) through a medium:



Wave: disturbance moves through medium - the medium itself has no overall motion

~~Caused~~ by: forces between neighbor molecules



electric attractive force $\sim$ spring

$\Rightarrow$ restoring force on each molecule

- disturbance propagates through medium.

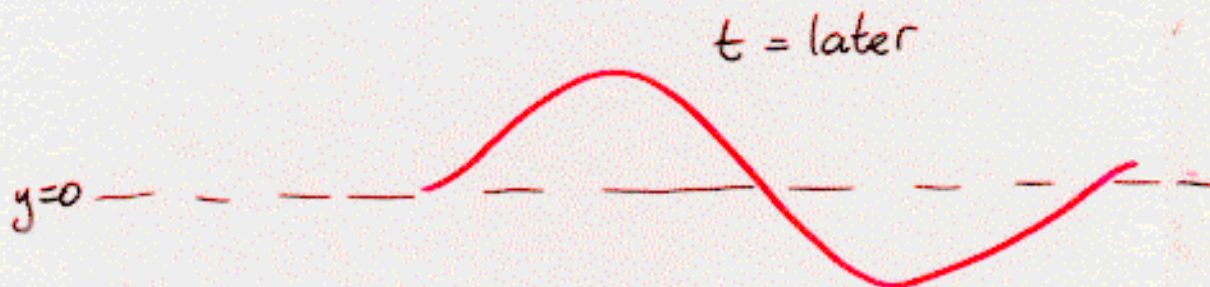
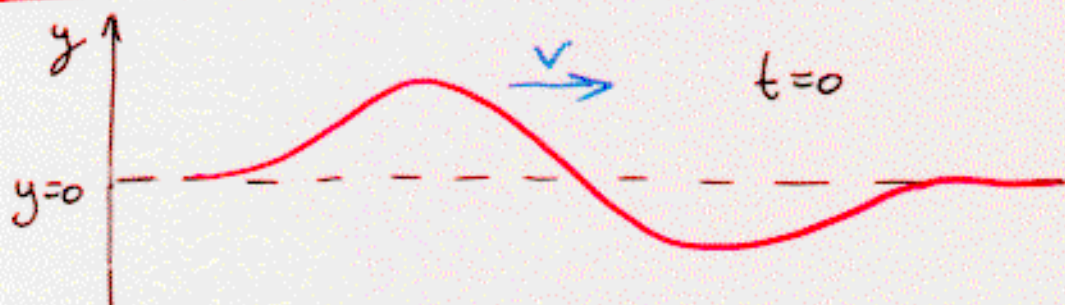
Wave Characteristics

Longitudinal : Displacement along direction of travel
(or compression waves) e.g. sound waves in fluids
(fluids cannot support shear forces, only compression/stretching)



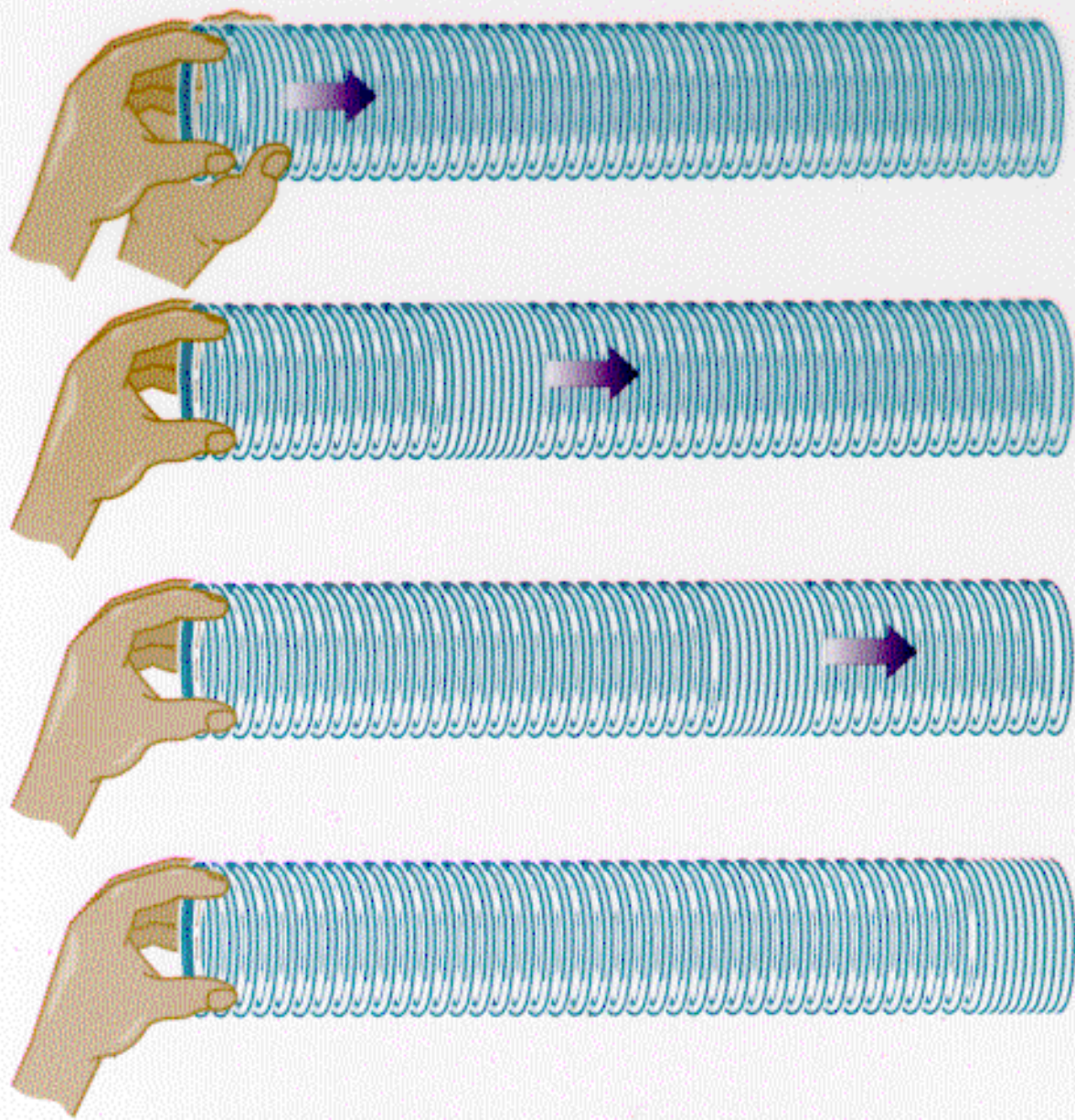
also solid bars, bones, earthquakes,

Transverse : Displacement $\perp$ to direction of travel

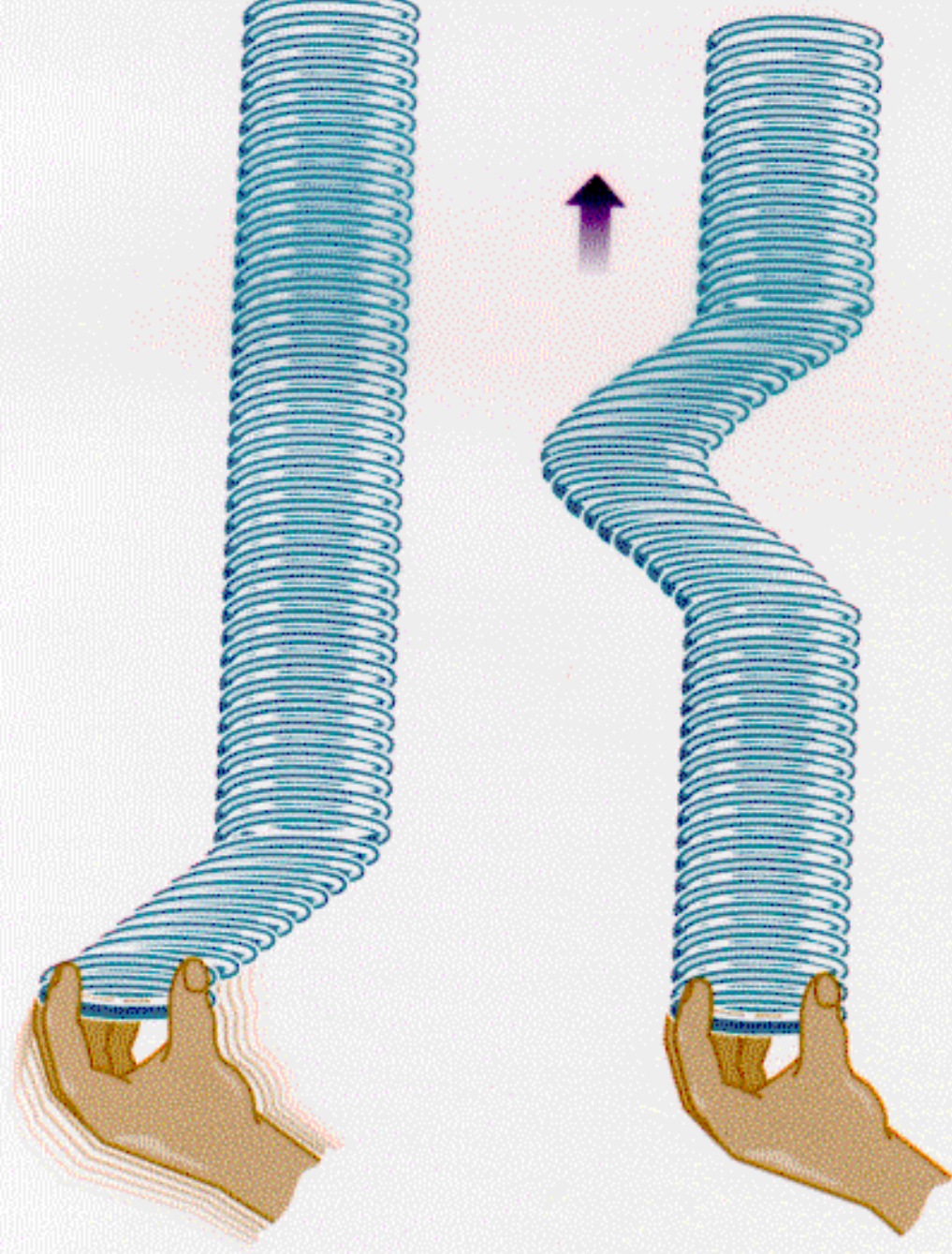


e.g. waves on rope, string, wires,
ocean surface,
earthquakes

Figure 11.2
Longitudinal wave in a spring



Transverse wave in a spring



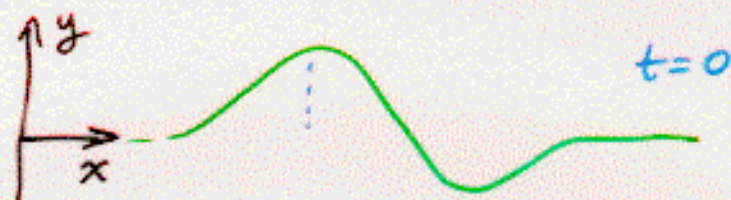
Wave forms

In general, point on (string, ocean) is displaced by wave depending on its position (x) and the time (t)

$\Rightarrow$ Wave function $\psi(x, t)$

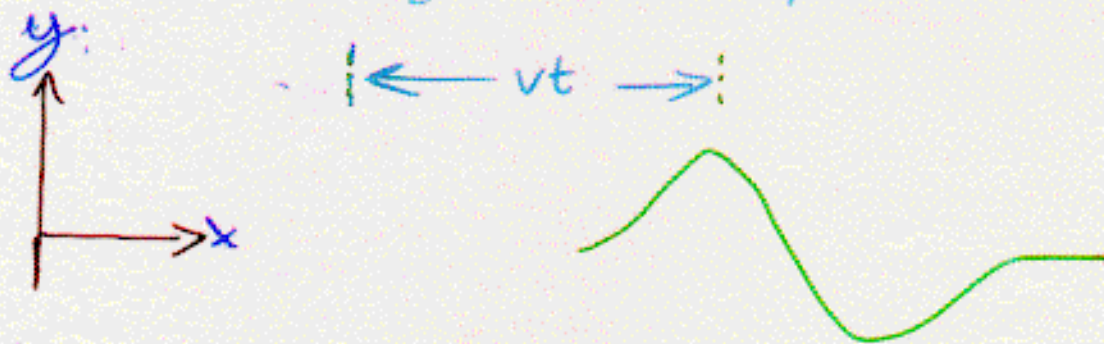
Can take "Snapshot" of displacement at a moment in time:

e.g.



$\Rightarrow$ displacement $y = \underline{f(x)}$ wave form

If wave form moves to right (x ?) at speed v :



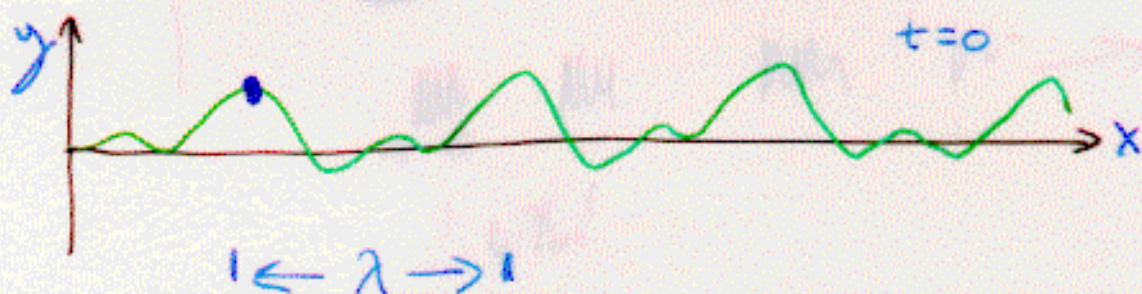
Now displacement $f(x) = f(x - vt)$

$\Rightarrow y = \psi(x, t) = \underline{\underline{f(x - vt)}}$

(For wave to left, $\psi(x, t) = f(x + vt)$)

Periodic Waves: Wavelength, Frequency

If wave-form repeats itself: (take snapshot)



Pattern repeats over a wavelength $= \lambda$ [m]

For point at fixed position x , motion is periodic
(e.g. string vibrates up+down)

As wave form passes through,

$$\text{repeat period } T = \frac{\text{repeat distance}}{\text{wave speed}} = \frac{\lambda \text{ [m]}}{v \text{ [m/s]}}$$

$$\therefore \text{Vibration freq. } f = \frac{1}{T} \text{ [Hz]} = \frac{v}{\lambda}$$

$$\Rightarrow \boxed{v = f \lambda}$$

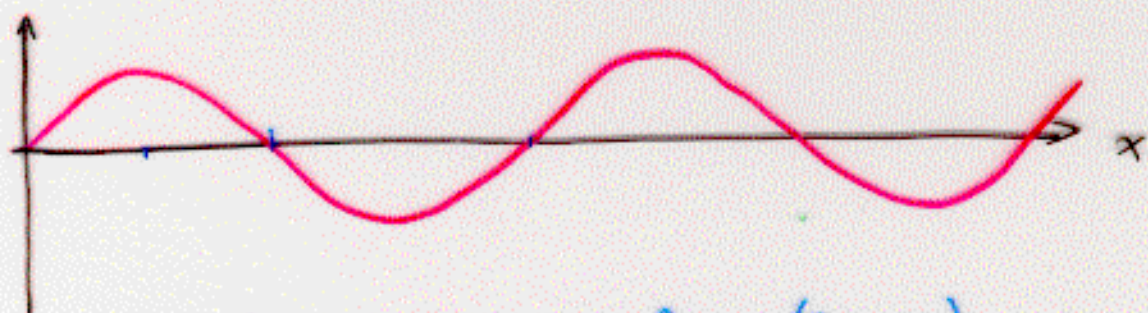
for any periodic wave

e.g. tuning fork vibrates at $f = 440 \text{ Hz}$, in air
Sound speed = 330 m/s

$$\Rightarrow \lambda = v/f = \frac{330 \text{ m/s}}{440 \text{ Hz}} = 0.75 \text{ m.}$$

Harmonic Waves

If each point on wave executes SHM,



Wave form is $y(x) = A \sin\left(2\pi \frac{x}{\lambda}\right)$

- repeats every 2π radians

i.e. $2\pi \frac{x}{\lambda} = 2\pi, 4\pi, \dots$

$\Rightarrow x = \lambda, 2\lambda, 3\lambda, \dots$ as required

For traveling wave $y(x) \rightarrow y(x-vt)$

So $y = A \sin \frac{2\pi}{\lambda} (x - vt)$: Harmonic Wave Equation.

Note: Since $v = f\lambda = \lambda/T$, this becomes

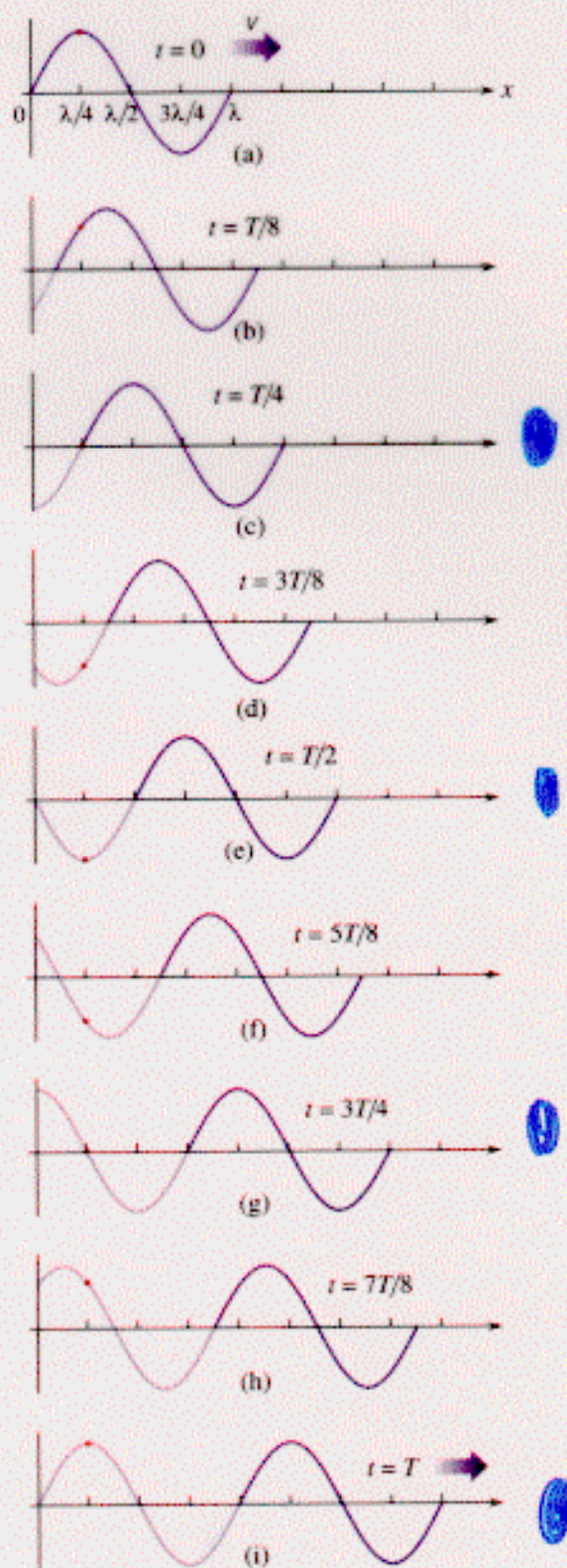
* $y = A \sin 2\pi \left(\frac{x}{\lambda} - \frac{t}{T} \right)$: repeats every λ and every period T .

[In general, depending on $y(t=0)$:

$y = A \sin \left[\frac{2\pi x}{\lambda} - 2\pi ft + \phi \right]$
[phase at $t=0$]

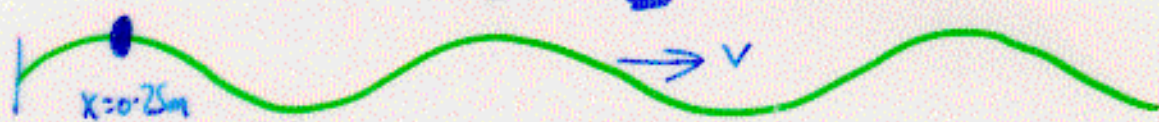
Figure 11.11

Harmonic wave moving along the x -axis



Example: A wave on a string is described by :

$$y = 0.02 \sin(6.28x - 15t) \quad \text{Find:}$$



1. Frequency and wavelength and speed of wave
2. Speed and acceleration of a bead on string at $x = 0.25m$

1. c.f. $y = A \sin\left(\frac{2\pi}{\lambda}(x - vt)\right)$

Here $y = 0.02 \sin(6.28(x - \frac{15}{6.28}t))$

$\Rightarrow$ amplitude $0.02m$, $\frac{2\pi}{\lambda} = 6.28$ so $\lambda = 1.0m$, $v = \frac{15}{6.28} = 2.39m/s$

2. For a point at $x = 0.25m$, disp. $y = 0.02 \sin(6.28 \times 0.25 - 15t)$
 $(= \frac{1}{4}\lambda)$

$$y = 0.02 \sin(1.57 - \frac{\omega}{15}t) *$$

= SHM with $\omega = 15 \text{ rad/s}$
 $A = 0.02m$.

So transverse speed of bead $\frac{dy}{dt} = -15 \times 0.02 \sin(1.57 - 15t)$

So max. speed = $A\omega = 15 \times 0.02 = 0.3m/s$

- unrelated to wave speed v .

Accel. of bead ($= \text{force/mass}$) $\frac{d^2y}{dt^2} = -\omega^2 y$

has max. accel = $(-)\omega^2 A = 15^2 \times 0.02 = 4.5m/s^2$