

Reading Quiz 4.

1. Impulse is a measure of:

a) energy

☒ b) momentum

c) change in energy

☒ d) change in momentum

Δmv

2. Two masses m_1, m_2 with $m_1 > m_2$ have the same momentum. Which has the greater kinetic energy?

a) Mass m_1

☒ b) Mass m_2

c) Both the same

d) Not enough info. given

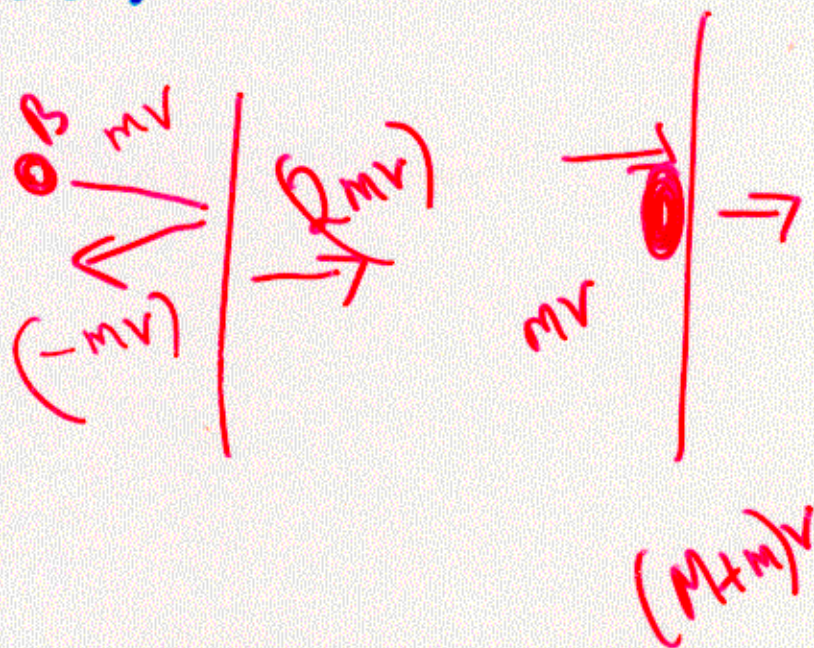
[Hint: $p = mv$ so $\frac{1}{2}mv^2 = \frac{p^2}{2m}$]

3. An INELASTIC collision is one in which the following are conserved:

- a) kinetic energy
- ☒ b) momentum
- c) relative speed
- d) All of the above.

4. A heavy wooden door can be opened by throwing a 0.25kg projectile at it. You can choose a billiard ball or a lump of Playdoh (clay). Which makes the door open faster?

- ☒ a) billiard ball
- b) lump of clay
- c) both the same
- d) Not enough info.



Momentum and Collisions (Ch 7)

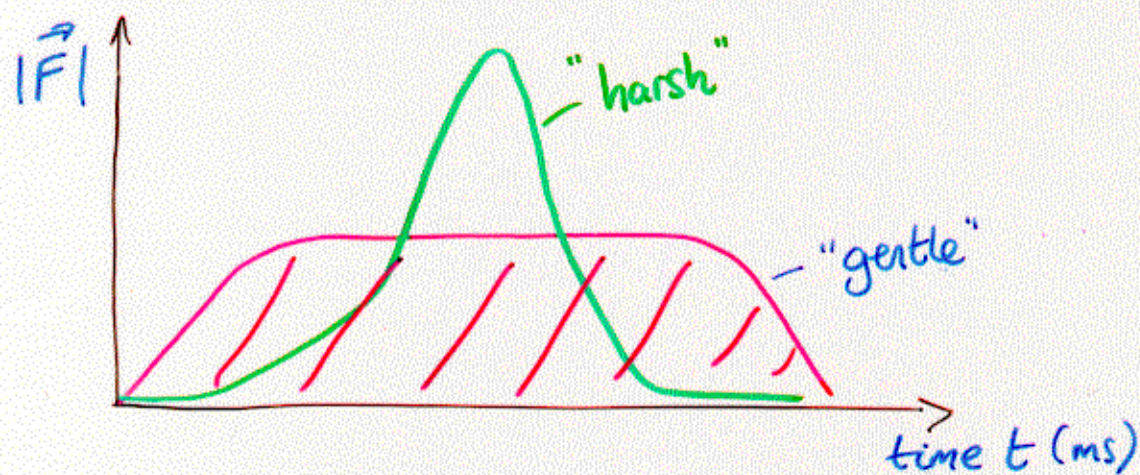
Impulse - change of momentum

From Newton II, $\vec{F} = \frac{d(m\vec{v})}{dt} = \frac{d\vec{p}}{dt}$

So force acting over time changes momentum

i.e. The impulse $\Delta\vec{p} = \int \vec{F} \cdot dt$

e.g. many ways to accelerate golf ball ($m = 0.05 \text{ kg}$)
up to $v = 60 \text{ m/s}$ from rest:



Both cases $\Rightarrow$ impulse $\int F \cdot dt = \Delta p = 0.05 \text{ kg} \times (60 - 0)$
 $= 3 \text{ kg m/s}$

Other examples: catch baseball with hand or table.

For same impulse, if time $\Delta t \downarrow$, $F_{\text{av}} \uparrow$ (ouch!)

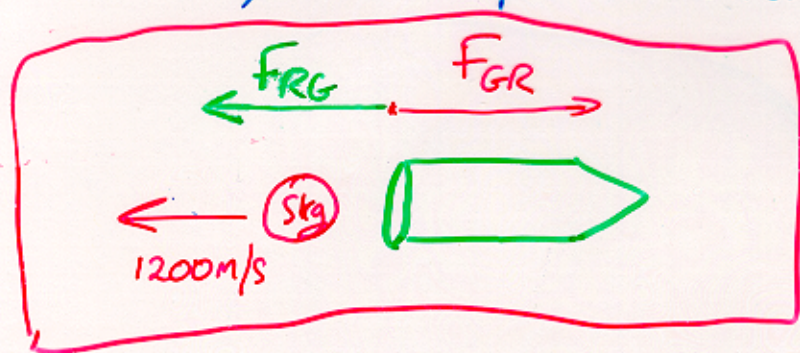
Newton's 3rd Law and Impulse

e.g. rocket expels gas at rate $\frac{dm}{dt} = 5 \text{ kg/s}$
with exhaust speed = 1200 m/s

In time $\Delta t = 1 \text{ s}$, impulse on 5 kg of gas

$$\underline{F_{av} \Delta t = 5 \text{ kg} \times 1200 \text{ m/s} = 6000 \text{ kg m/s}}$$

$\therefore$ From Newton III, reaction force on rocket = $|F_{av}| = 6000 \text{ kg m/s}^2 = 6000 \text{ N}$.



$\therefore$ In 1 s , impulse on rocket = - impulse on gas

$$(\Delta mv)_{\text{rocket}} = -(\Delta mv)_{\text{gas}}$$

$$\Rightarrow \text{total momentum change } (\Delta mv)_{\text{rocket}} + (\Delta mv)_{\text{gas}} = 0.$$

Conservation of Linear Momentum

Principle: When no net external force on system, the momentum of the system is conserved (i.e. stays constant, $\Delta \vec{P} = 0$)

$$\vec{P} = m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots$$

e.g. Two masses collide



During collision, at any instant $F_{AB} = -F_{BA}$ (Newton III)

and time interval $\Delta t_A = \Delta t_B$

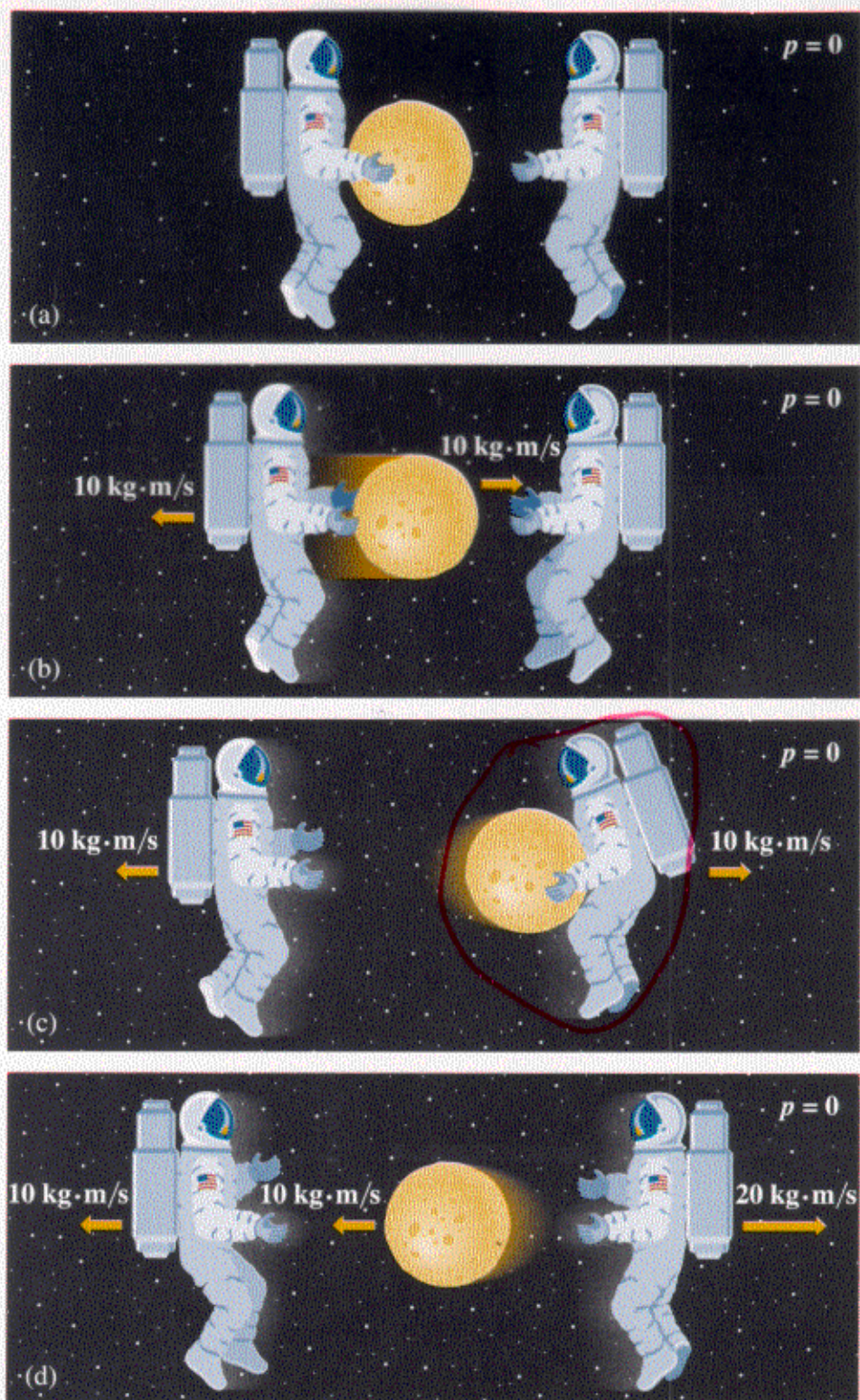
$$\therefore \text{Impulse on A} = \int F_{BA} dt = -\text{Impulse on B} \int F_{AB} dt$$
$$\Delta(m_A v_A) = -(\Delta m_B v_B)$$

$$\Rightarrow \Delta P = \Delta(m_A v_A) + \Delta(m_B v_B) = 0$$

Note: Add friction $\Rightarrow$ net external force on system
 $\Rightarrow$ momentum no longer conserved.

Figure 7.9

Conservation of linear momentum



Same result as long as $\int F \cdot dt = 10 \text{ kg} \cdot \text{m/s}$

- "gentle" or "harsh" throw or catch makes no difference