

11.3

Use Eq. (11.1) to solve for λ , with $v = 1498 \text{ m/s}$ and $f = 440 \text{ Hz}$:

$$\lambda = \frac{v}{f} = \frac{1498 \text{ m/s}}{440 \text{ Hz}} = 3.40 \text{ m}.$$

11.5

For a periodic wave of wavelength λ , wave speed v and frequency f , Eq. (11.1) holds true: $v = f\lambda$. Rewrite this as $f = v/\lambda$ and multiply both sides by 2π to obtain $2\pi f = 2\pi v/\lambda = (2\pi/\lambda)v$. But $2\pi f = \omega$ (the angular frequency of the wave), so $\omega = (2\pi/\lambda)v$.

11.17

In order not to be masked by the next group of chirps, a wavetrain must make it from the bat to the object (which is located a distance x away) and get reflected back to the bat in a time interval no longer than $\Delta t = 70 \text{ ms}$. Thus if the speed of the wavetrain is v , then for the round-trip the total distance $2x$ must satisfy $2x/v \leq \Delta t$, or

$$x_{\max} = \frac{1}{2} v \Delta t = \frac{1}{2} (330 \text{ m/s}) (70 \times 10^{-3} \text{ s}) = 12 \text{ m}.$$

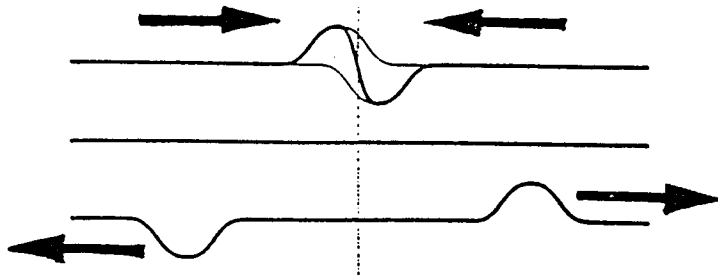
11.29

Use Eq. (11.4), $v = \sqrt{F_T/\mu}$, to find F_T . Here $v = 129 \text{ m/s}$ and $\mu = 64.9 \times 10^{-3} \text{ kg/m}$ is the linear mass-density. Thus

$$F_T = v^2 \mu = (129 \text{ m/s})^2 (64.9 \times 10^{-3} \text{ kg/m}) = 1.08 \times 10^3 \text{ N}.$$

11.31

Similar to the previous problem, suppose that the picture in the text (Fig. P31) was taken at $t = 0$. In the following sequence, the top figure depicts the situation a little before $t = 2 \text{ s}$, the middle one is the picture at exactly $t = 2 \text{ s}$ (when the two peaks coincide), while the bottom one is at $t = 4 \text{ s}$.



11.35

If the amplitude of a harmonic wave is A and its frequency is f , then each particle in the medium carrying the wave is in a simple harmonic motion with the same frequency and amplitude. According to Eq. (10.17) the maximum acceleration of each particle in the wave is then $a_{\max} = [-\omega^2 A \cos \omega t]_{\max} = \omega^2 A = (2\pi f)^2 A$. In this case, the waveform is $y = 0.040 \sin(2\pi x)$ which, when compared with the standard form in Eq. (11.2), $y = A \sin(2\pi x/\lambda)$, yields $A = 0.040$ m and $\lambda = 1.0$ m. Thus

$$a_{\max} = (2\pi f)^2 A = \left(\frac{2\pi v}{\lambda}\right)^2 A = \left[\frac{2\pi(2.0 \text{ m/s})}{1.0 \text{ m}}\right]^2 (0.040 \text{ m}) = 6.3 \text{ m/s}^2,$$

where we used $f = v/\lambda$.

11.37

The wave speed v is obtained from Eq. (11.4):

$$v = \sqrt{\frac{F_T}{\mu}} = \sqrt{\frac{25.0 \text{ N}}{2.50 \times 10^{-3} \text{ kg/m}}} = 100 \text{ m/s};$$

the angular speed ω is given by $\omega = 2\pi f = 2\pi(50.0 \text{ Hz}) = 314 \text{ rad/s}$; the period is $T = 1/f = 1/50.0 \text{ Hz} = 0.0200 \text{ s}$; and the wavelength is $\lambda = v/f = (100 \text{ m/s})/50.0 \text{ Hz} = 2.00 \text{ m}$.

11.47

Solve for Y from Eq. (11.7), $v = \sqrt{Y/\rho}$:

$$Y = \rho v^2 = (19.3 \times 10^3 \text{ kg/m}^3)(4319 \text{ m/s})^2 = 3.60 \times 10^{11} \text{ Pa} = 360 \text{ GPa}.$$

11.61

As the needle moves through the groove it encounters a total of 1.5×10^3 wiggle-wavelengths each second, producing a sound of frequency $f = 1.5 \times 10^3 \text{ Hz} = 1.5 \text{ kHz}$. Since the needle traverses 0.50 m during each second, there must be 1.5×10^3 wiggle-wavelengths in 0.50 m . Thus the wiggle-wavelength is $\lambda = 0.50 \text{ m}/(1.5 \times 10^3) = 3.3 \times 10^{-4} \text{ m} = 0.33 \text{ mm}$.

11.63

The period T of the middle-C is $T = 1/f = 1/261.6 \text{ Hz} = 3.823 \times 10^{-3} \text{ s} = 3.823 \text{ ms}$. Thus the contact time for the note is $\frac{1}{2}(3.823 \text{ ms}) = 1.911 \text{ ms}$, or, to two significant figures, 1.9 ms .

11.93

For the first system the sound-level is $\beta_1 = 10 \log_{10}(I_1/I_0)$, while for the second one (the one with greater acoustic power output) $\beta_2 = 10 \log_{10}(I_2/I_0)$. The difference in their sound-levels is then

$$\begin{aligned} \Delta\beta &= 10 \log_{10} \left(\frac{I_2}{I_0} \right) - 10 \log_{10} \left(\frac{I_1}{I_0} \right) = 10 \log_{10} \left[\left(\frac{I_2}{I_0} \right) / \left(\frac{I_1}{I_0} \right) \right] \\ &= 10 \log_{10} \left(\frac{I_2}{I_1} \right) = 10 \log_{10} \left(\frac{10I_1}{I_1} \right) \\ &= 10 \log_{10}(10) = 10 \text{ dB}. \end{aligned}$$

Note that we used the identity $\log_a x - \log_a y = \log_a(x/y)$.

11.95

The sound-level β is related to the intensity I by Eq. (11.10): $\beta = 10 \log_{10}(I/I_0)$. Since the two systems have the same intensity at the location of the microphone, they must also have the same sound-level. The difference in their sound-levels is therefore 0 dB.

11.99

Apply the result of the previous problem: $I = 10^{\beta/10} I_0$. In this case $\beta = 77$ dB, so

$$I = 10^{\beta/10} I_0 = (10^{77/10})(10^{-12} \text{ W/m}^2) = 5.0 \times 10^{-5} \text{ W/m}^2.$$

11.103

At $R = 5.0$ m from the source

$$\beta = 10 \log_{10} \left(\frac{I}{I_0} \right) = 10 \log_{10} \left(\frac{56 \times 10^{-5} \text{ W/m}^2}{10^{-12} \text{ W/m}^2} \right) = 87 \text{ dB}.$$

Since $I \propto R^{-2}$ for spherical waves, At $R' = 20.0$ m from the printer the intensity drops to $I' = I(R/R')^2 = I(5.0 \text{ m}/20.0 \text{ m})^2 = 0.0625 I$, and the sound-level changes by

$$\Delta\beta = 10 \log_{10} \left(\frac{I'}{I} \right) = 10 \log_{10} \left(\frac{0.0625 I}{I} \right) = -12 \text{ dB},$$

so the sound-level there is $\beta' = \beta + \Delta\beta = 87 \text{ dB} + (-12 \text{ dB}) = 75 \text{ dB}$.

11.109

The sound intensity I varies as the square of the acoustic pressure P : $I \propto P^2$. Thus $I/I_0 = (P/P_0)^2$, where $P_0 = 2 \times 10^{-5}$ Pa corresponds to an intensity of I_0 . Thus from Eq. (11.10)

$$\beta = 10 \log_{10} \left(\frac{I}{I_0} \right) = 10 \log_{10} \left(\frac{P}{P_0} \right)^2 = 20 \log_{10} \left(\frac{P}{P_0} \right).$$

11.115

According to the problem statement the period of the beats is $T_{\text{beat}} = 0.99$ s, so the beat frequency is $f_{\text{beat}} = 1/T_{\text{beat}} = 1/0.99 \text{ s} = 1.0$ Hz, which is the same as Δf , the difference in frequency between the two tuning forks which produce the beats.

11.119

First, find the speed v of the wave on the piano string of length L and mass m under tension F_T using Eq. (11.4), $v = \sqrt{F_T/\mu}$, where μ is the linear mass-density of the string:

$$v = \sqrt{\frac{F_T}{\mu}} = \sqrt{\frac{100 \text{ N}}{2.5 \times 10^{-3} \text{ kg}/1.00 \text{ m}}} = 2.0 \times 10^2 \text{ m/s}.$$

Also, the wavelength λ_1 of the fundamental mode is given by Eq. (11.14), with $N = 1$: $\lambda_1 = 2L/1 = 2(1.00 \text{ m})/1 = 2.00$ m. Thus the corresponding frequency f_1 is

$$f_1 = \frac{v}{\lambda_1} = \frac{2.0 \times 10^2 \text{ m/s}}{2.00 \text{ m}} = 1.0 \times 10^2 \text{ Hz} = 0.10 \text{ kHz}.$$

11.130

Similar to the previous problem, it is clear that the wavelength λ_1 of the fundamental mode will not change as a result of temperature change, since λ_1 depends only on the length of the tube, which is assumed to be a constant. Thus $f_1 = v/\lambda_1 \propto v$. At 0°C the speed of sound is $v = 331.5\text{ m/s}$, while at 40°C it becomes $v' = 331.5\text{ m/s} + (0.60\text{ m/s}^\circ\text{C})(40^\circ\text{C}) = 355.5\text{ m/s}$. Thus the frequency f' at 40°C satisfies $f'_1/f_1 = v'/v$, or

$$f'_1 = f_1 \left(\frac{v'}{v} \right) = (200\text{ Hz}) \left(\frac{355.5\text{ m/s}}{331.5\text{ m/s}} \right) = 214\text{ Hz},$$

which is higher than f_1 (at 0°C) by 14 Hz.

11.145

The beat frequency, f_{beat} , is the difference between f_s , the source frequency; and f_o , the observed frequency of the reflected signal. According to Eq. (11.23) $f_o = f_s(v + v_t)/(v - v_t)$, where v_t is the speed of the target approaching the observer. So the beat frequency is

$$f_{\text{beat}} = f_o - f_s = f_s \left(\frac{v + v_t}{v - v_t} \right) - f_s = \frac{2v_t f_s}{v - v_t}.$$